

# Jet substructure in Heavy Ion Collisions

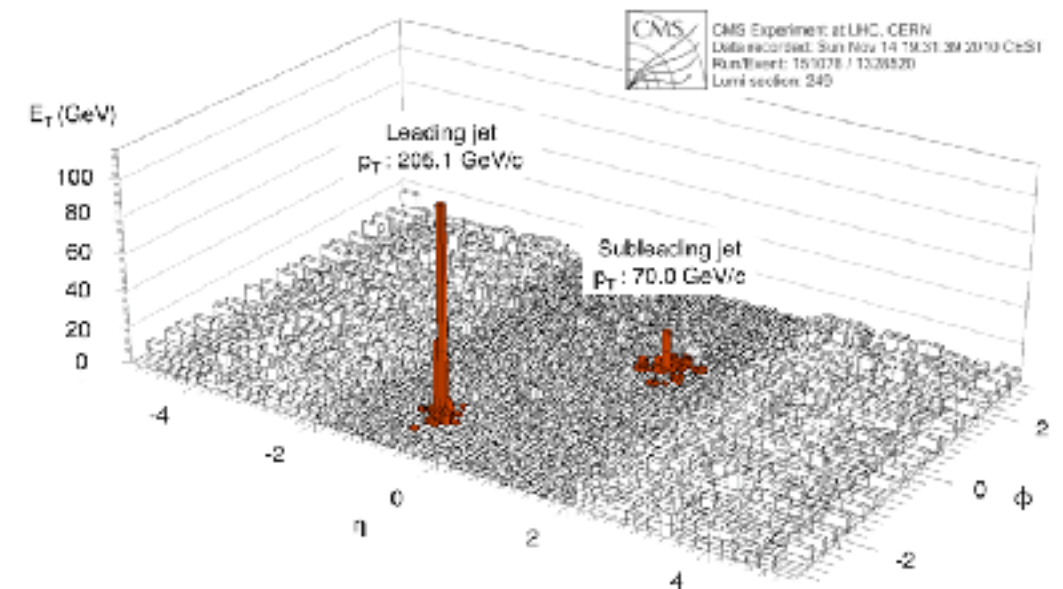
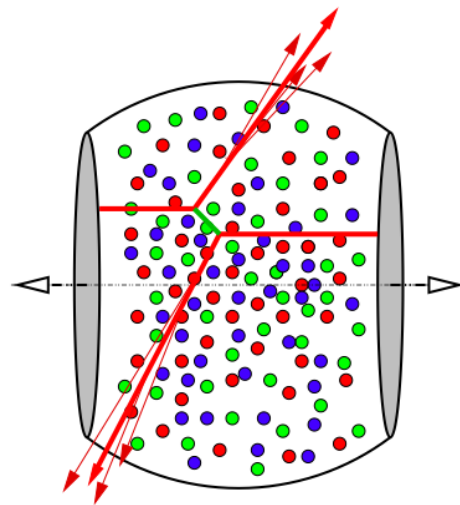
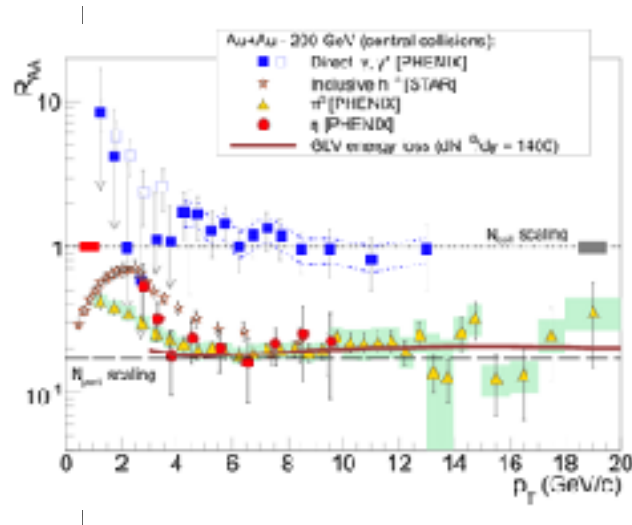
Sensitivity to medium-induced radiation and  
color decoherence

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RBRC Workshop, Feb 12-14, 2017  
@ BNL

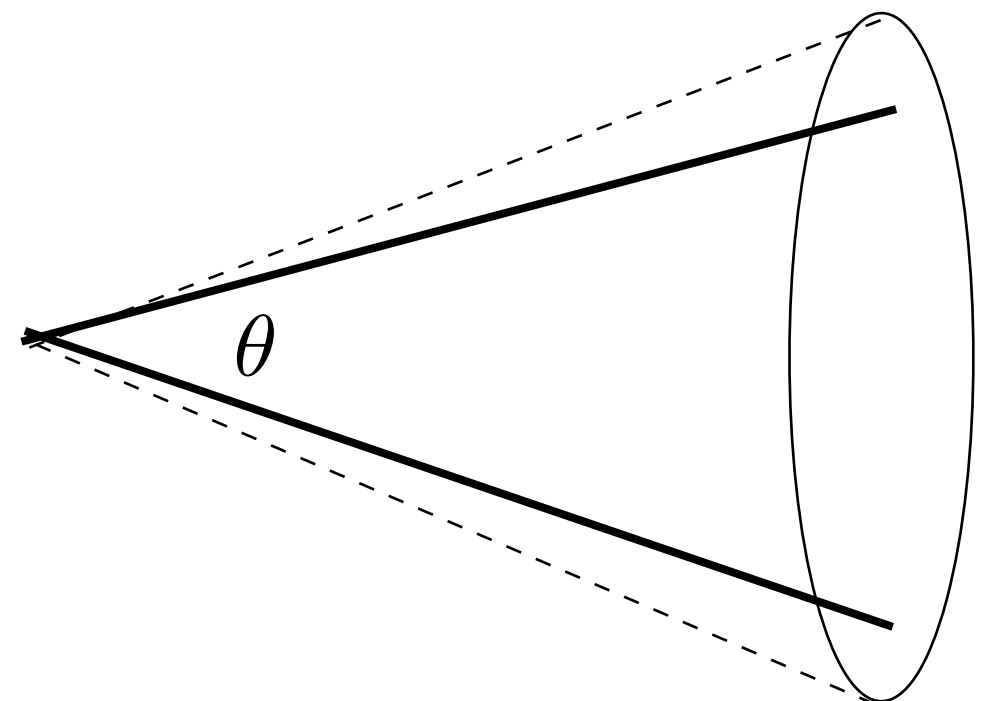
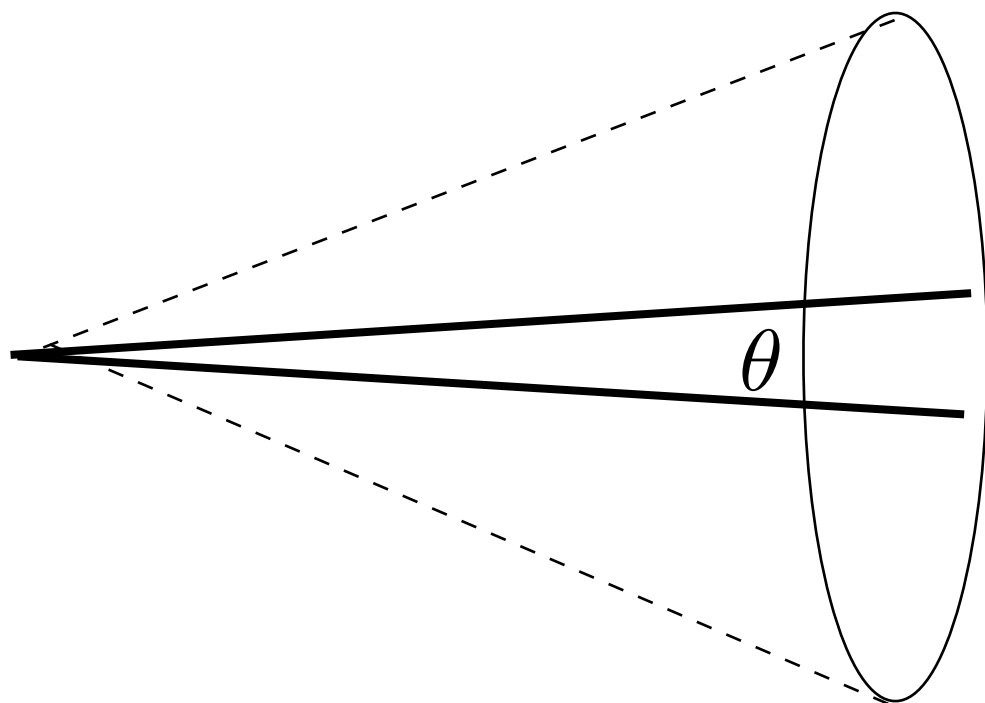
# Probing the quark-gluon-plasma with jets

from  
inclusive Jet observables



to Jet (sub)structure  
(angular distribution, fragmentation  
functions, jet shapes, etc)

- Use jet substructure techniques to investigate the transition from color **coherence** to **decoherence** by varying the angle between subjects:



Energy loss dependence on the angular separation?

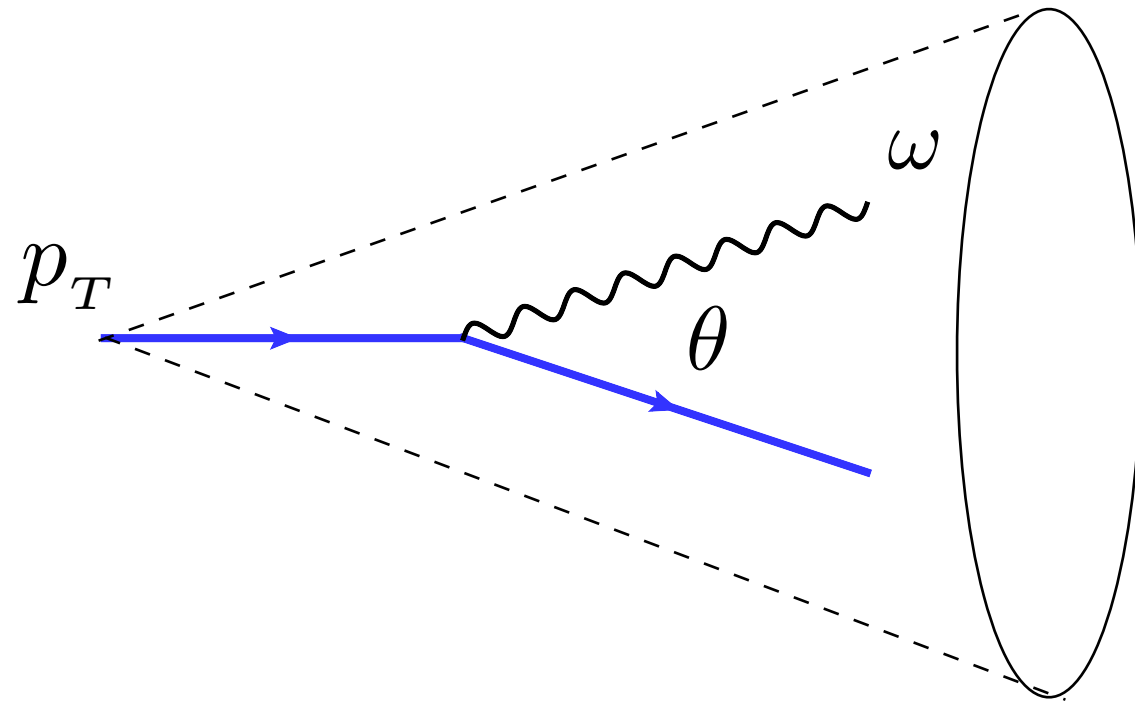
Jets from pQCD



# Jets in pQCD

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- Building block probability for parton cascades in vacuum



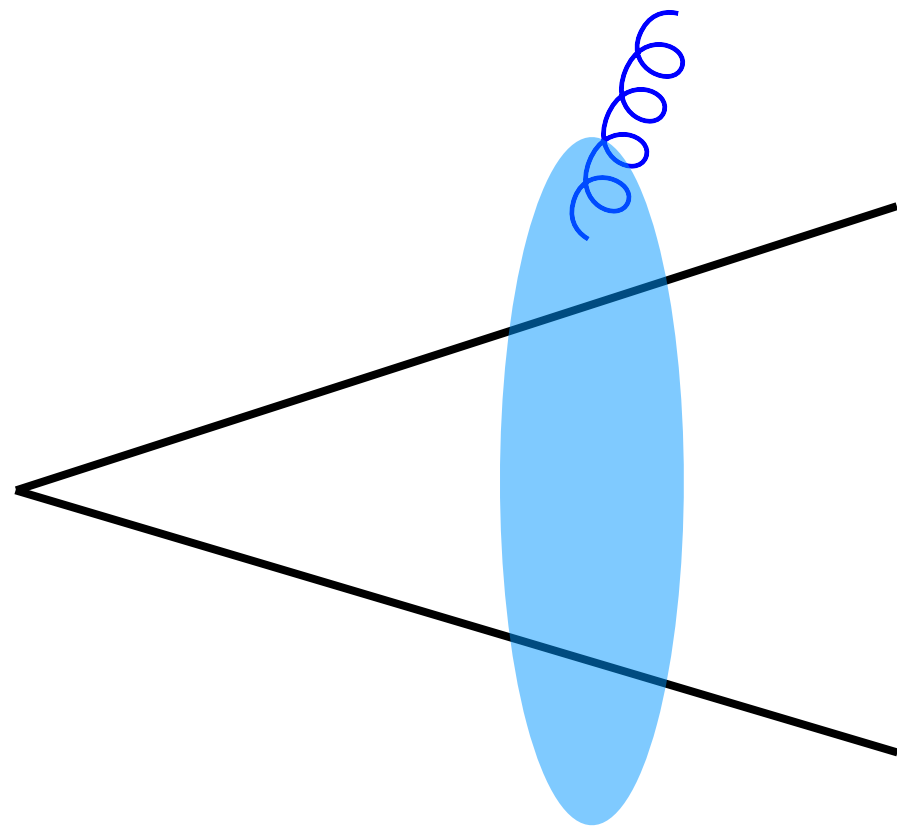
$$dP \sim \alpha_s C_R \frac{d\theta}{\theta} \frac{d\omega}{\omega} \quad \Rightarrow \text{collimation of jets}$$

Large phase space for multiple branching: many particles  
Produced (Implemented in Event generators such as  
PYTHIA, HERWIG, SHERPA, etc.)

# Jets in pQCD

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- Building block probability for parton cascades in vacuum



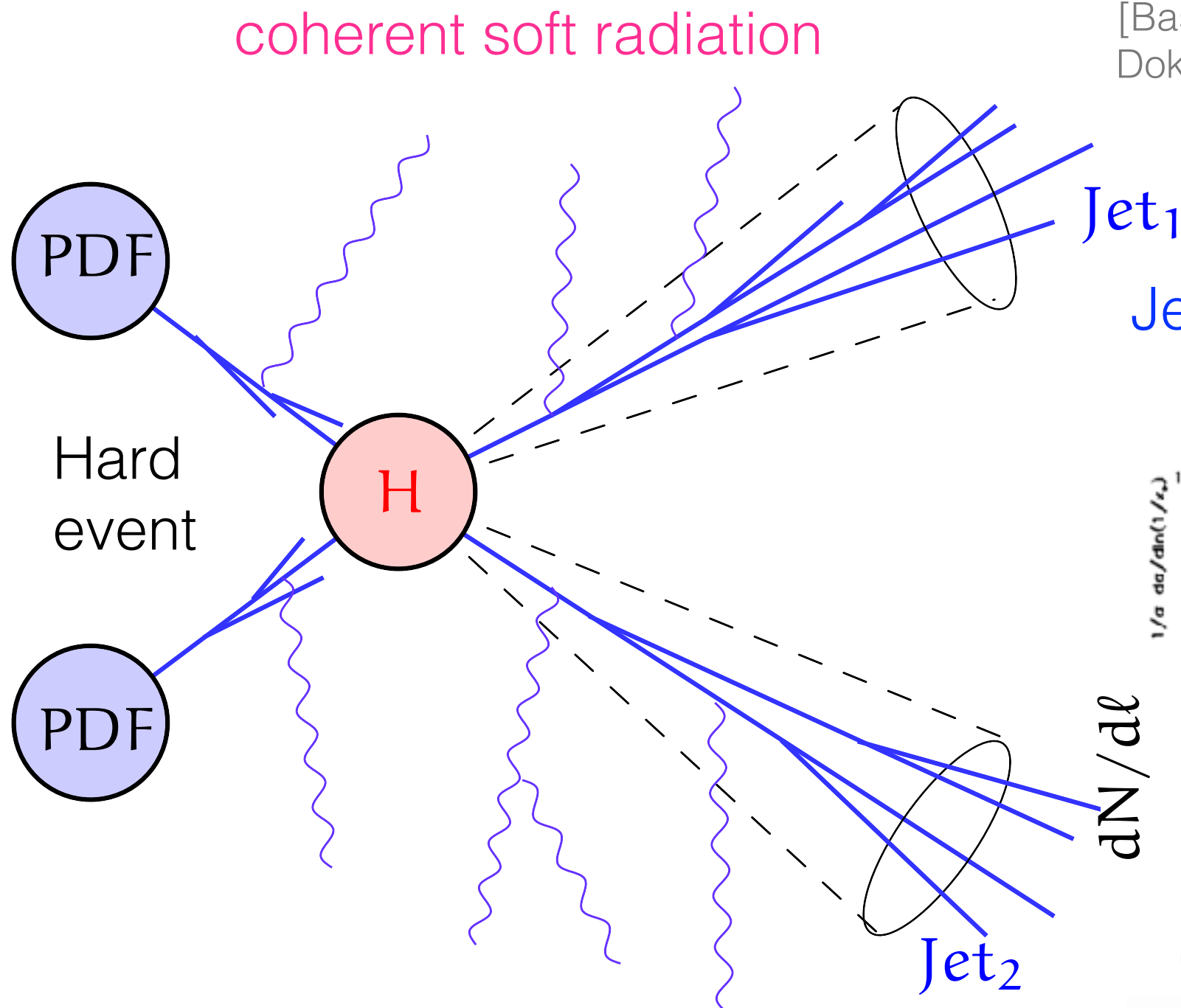
large angle radiation is  
suppressed  
(sensitive to **total color charge**)

- Radiation pattern for a color singlet Antenna :

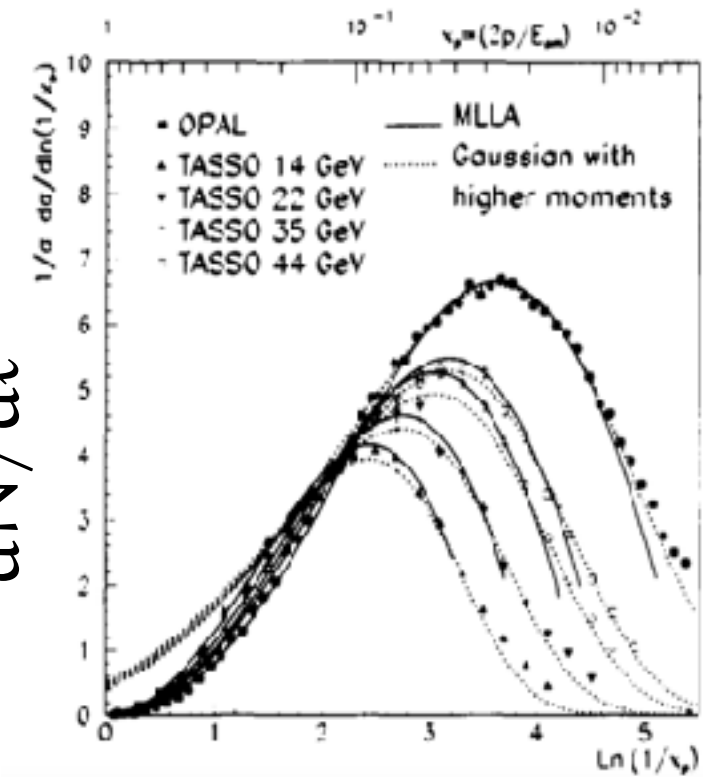
$$dP \sim \alpha_s C_R \frac{d\theta}{\theta} \frac{d\omega}{\omega} \Theta(\theta_0 - \theta)$$

# Jet in pQCD (color coherence)

[Bassetto, Ciafaloni, Marchesini, Mueller, Dokshitzer, Khoze, Toyon, Collins, Soper, Sterman ... 1980's]



Jet function (universal)  
collinear splittings

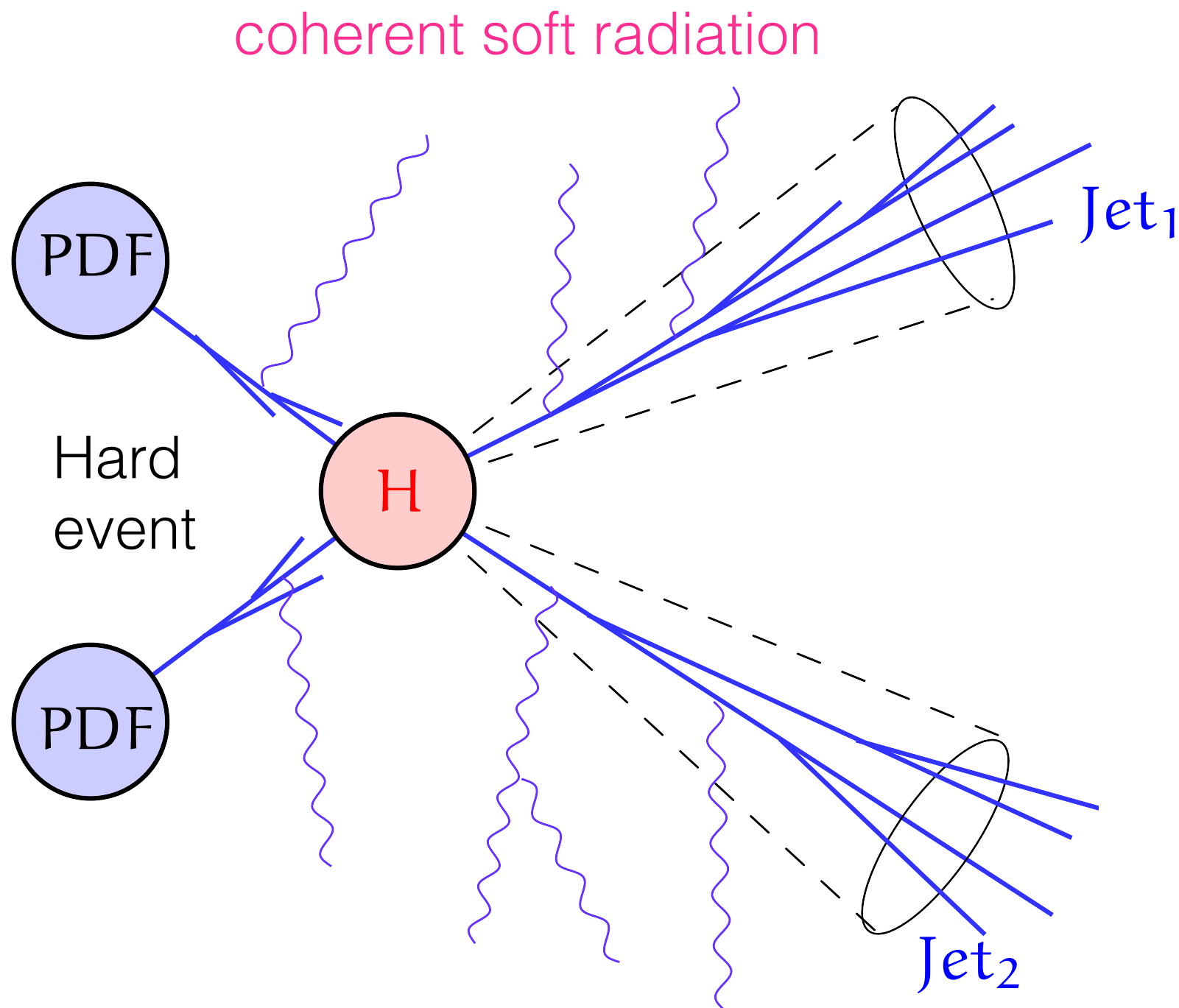


$$\ell = \ln \frac{1}{z}$$

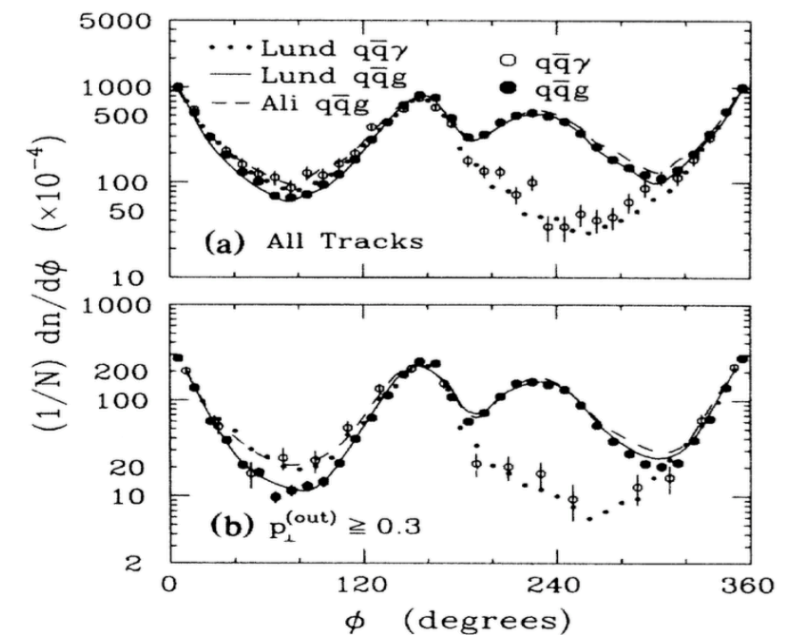
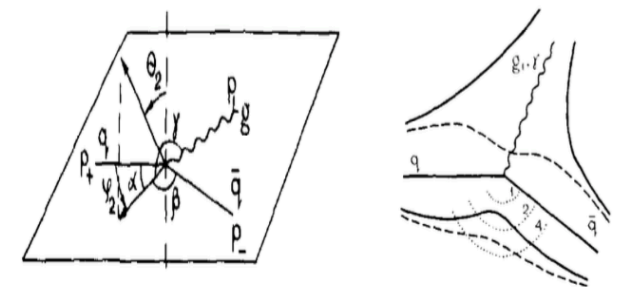
Factorization of the cross-section

$$\sigma \sim \text{PDF} \times H \times J_1 \times J_2 \times S$$

# Jet in pQCD (color coherence)



Interjet hadronic activity: “Stringy” fragmentation from pQCD



Factorization of the cross-section

$$\sigma \sim \text{PDF} \times H \times J_1 \times J_2 \times S$$

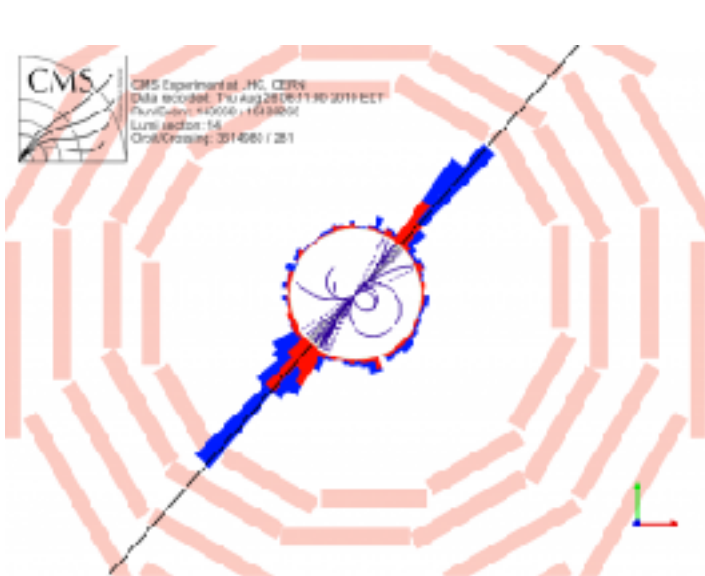
# Jet observables of two types

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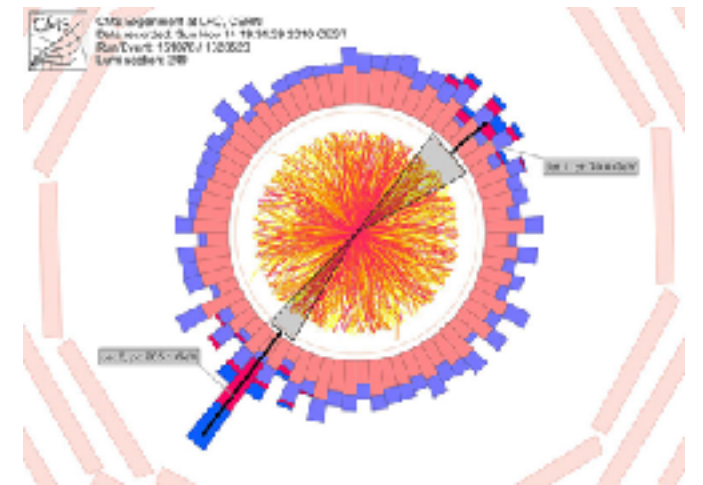
- Infrared-Collinear (IRC) safe observables: sum over final state hadrons  $\rightarrow$  cancellations of divergences. Ex: event shape: thrust, jet mass, jet spectra, etc. Resummation of large logs, e.g.  $\log R$  can be necessary
- Collinear sensitive observables: pQCD still predictive (factorization theorems). Ex: Fragmentation Functions

# Jets in pQCD (high precision)

# Parton Energy loss



?

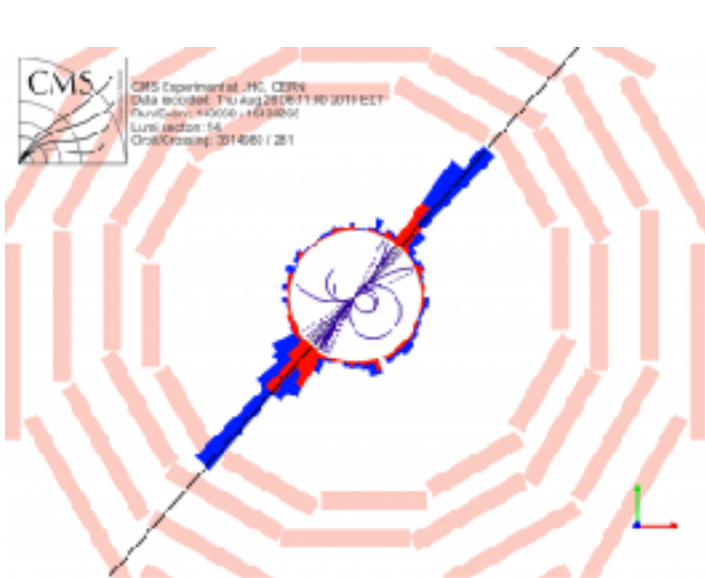


## Theory of jets in the plasma

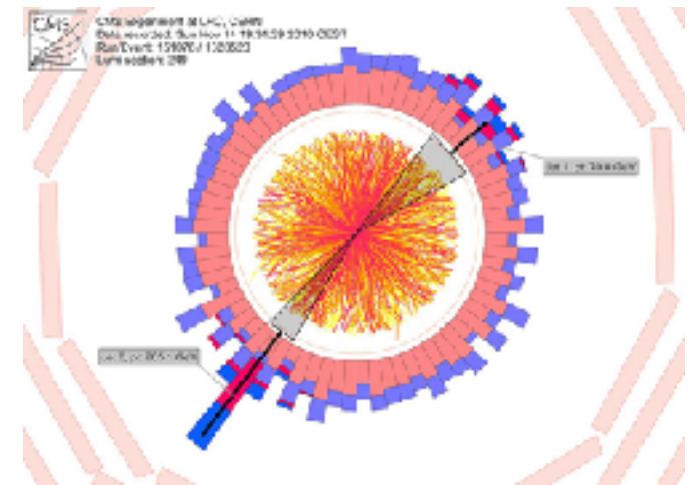
- (i) Parton cascade of two kinds  
(vacuum and medium induced)
- (ii) Color decoherence

# Jets in pQCD (high precision)

# Parton Energy loss



?



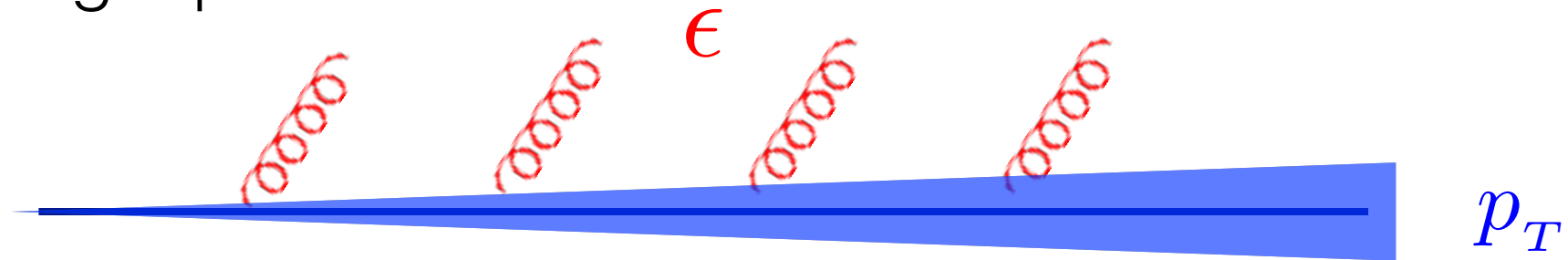
## Theory of jets in the plasma

⇒ Also important for the problem of  
thermalization in HIC

# Jet quenching and fluctuations

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- Standard energy loss picture: **medium-induced radiation** off a single parton



- Energy loss probability for large media

$$D(\epsilon) \equiv \frac{\sqrt{\omega_{\text{br}}}}{\epsilon^{3/2}} e^{-\frac{\pi \omega_{\text{br}}}{\epsilon}} \quad \omega_{\text{br}} \equiv \bar{\alpha}^2 \hat{q} L^2$$

[Baier, Dokshitzer, Mueller, Schiff, JHEP (2001) Jeon, Moore (2003)]

- Single scale: large fluctuations of energy loss
- Medium properties encoded in the jet quenching parameter

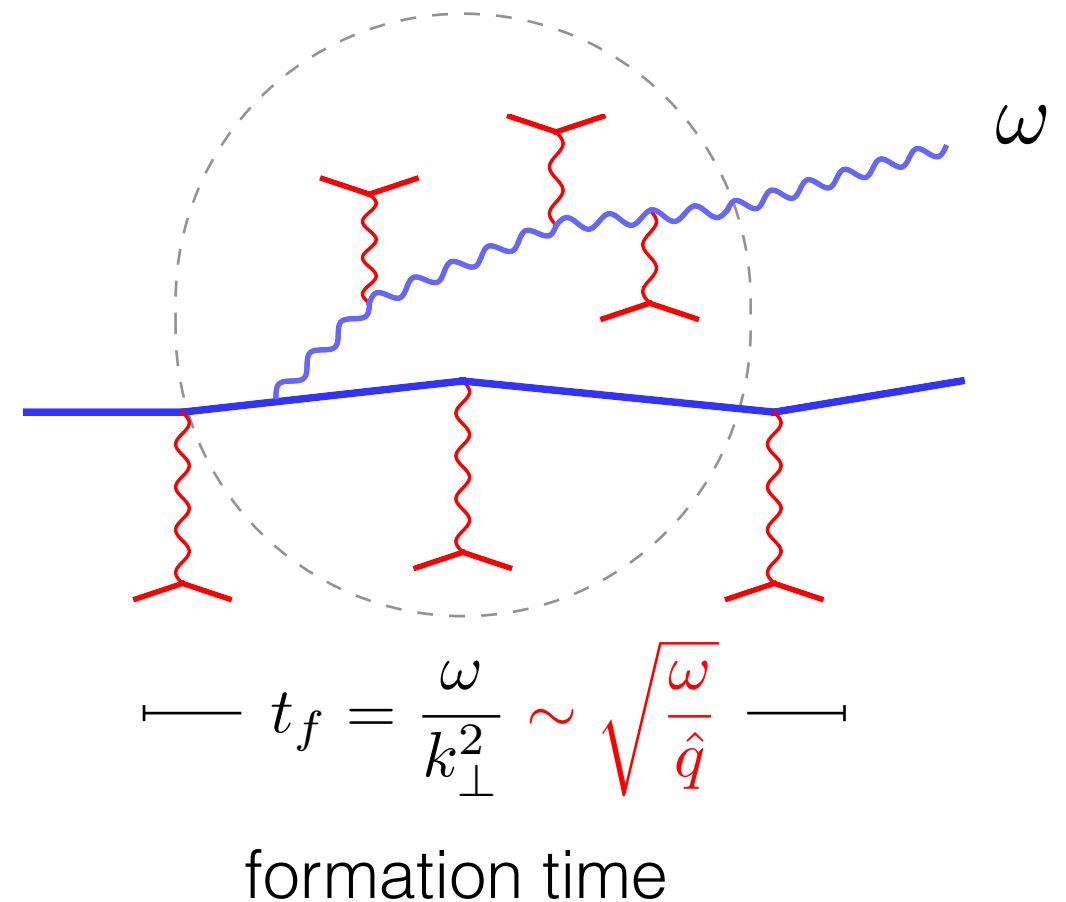
$$\hat{q} \sim \frac{\langle k_{\perp}^2 \rangle}{L}$$



# Longitudinal coherence (LPM effect)

- Radiation triggered by multiple scatterings
- Landau-Pomeranchuk-Migdal suppression (coherent radiation)

$$\omega \frac{dI}{d\omega} = \alpha_s C_R \sqrt{\frac{\omega_c}{\omega}}$$



- Maximum suppression when  $t_f \gtrsim L \Rightarrow \omega > \omega_c = \hat{q}L^2$
- Minimum radiation angle  $\theta > \theta_c \equiv 1/\sqrt{\hat{q}L^3}$

[Baier, Dokshitzer, Mueller, Peigné, Schiff (1995-2000) Zakharov (1996)]

[Wiedemann (2001) Arnold, Moore, Yaffe (2002)]

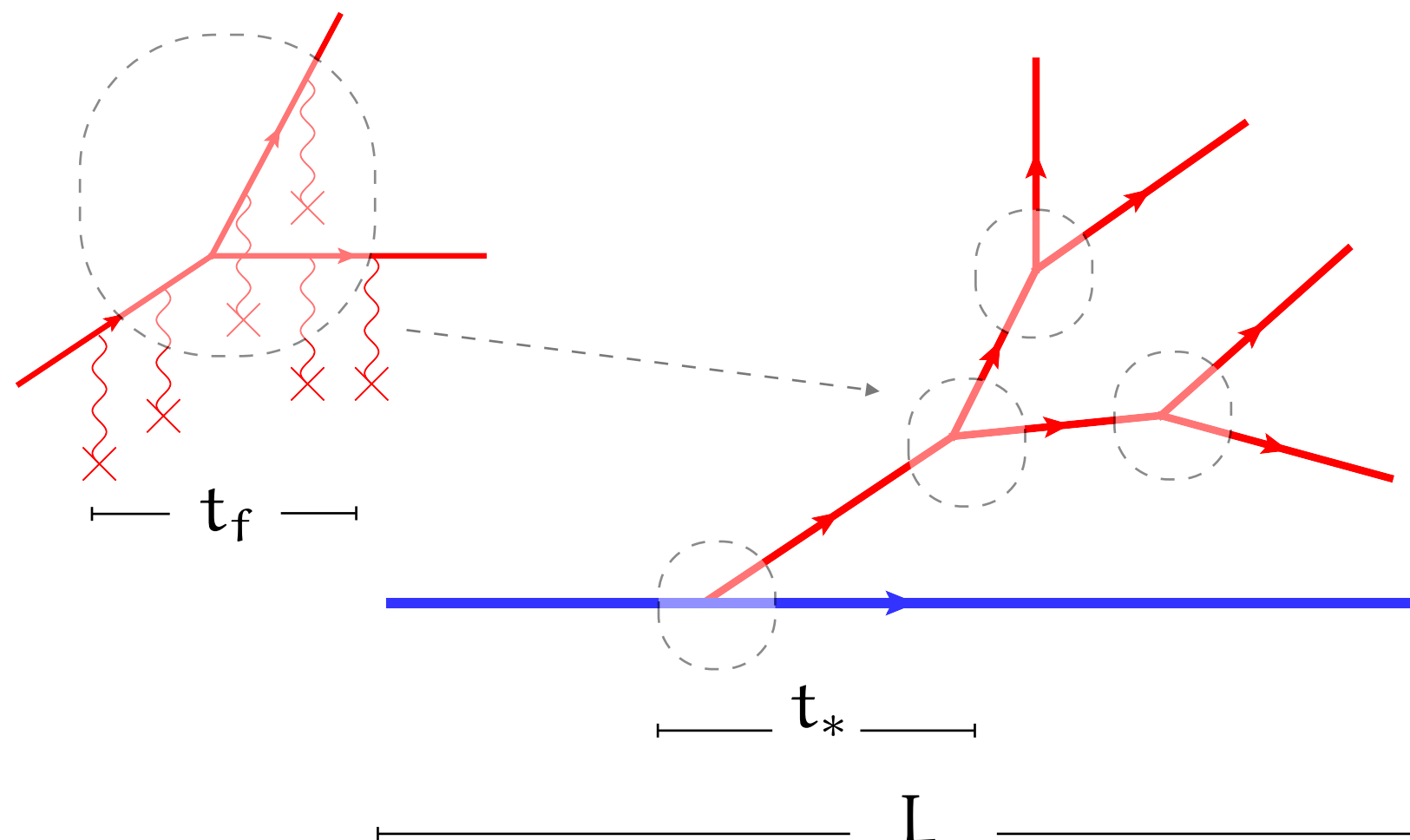
# Probabilistic picture of in-medium cascade

- Multiple (independent) branchings regime:

$$t_f \ll t_{\text{br}} \ll L$$

- Incoherent branchings: randomization of color due to rescatterings

[Blaizot, Dominguez, Iancu, MT (2013-2014)]



branching time

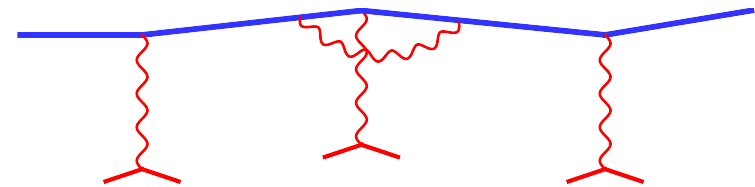
$$t_{\text{br}}(\omega) \sim \frac{1}{\alpha_s} t_f(\omega)$$

# Renormalization of the jet quenching parameter

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- Radiative corrections to pt-broadening to DLA accuracy

$$\langle k_{\perp}^2 \rangle \simeq \hat{q} L \left( 1 + \frac{\alpha_s N_c}{2\pi} \ln^2 \frac{L}{\tau_0} \right)$$



[Wu (2011) Liou, Mueller, Wu (2014) Blaizot, Iancu, Dominguez, MT (2014)]

- The double log can be absorbed in a redefinition of  $\hat{q}$

$$\hat{q} \equiv \hat{q}_0 \left( 1 + \frac{\alpha_s N_c}{2\pi} \ln^2 \frac{L}{\tau_0} \right)$$

[Blaizot, MT (2014)]

Eloss anomalous scaling:  $\Delta E \sim L^{2+\gamma}$  with  $\gamma \equiv \sqrt{\frac{4\alpha_s N_c}{\pi}}$

Between the plain pQCD  $L^2$  and AdS/CFT results  $L^3$

[Gubser et al, Hatta et al, Chesler et Yaffe (2008)] 15

# Energy flow at large angle

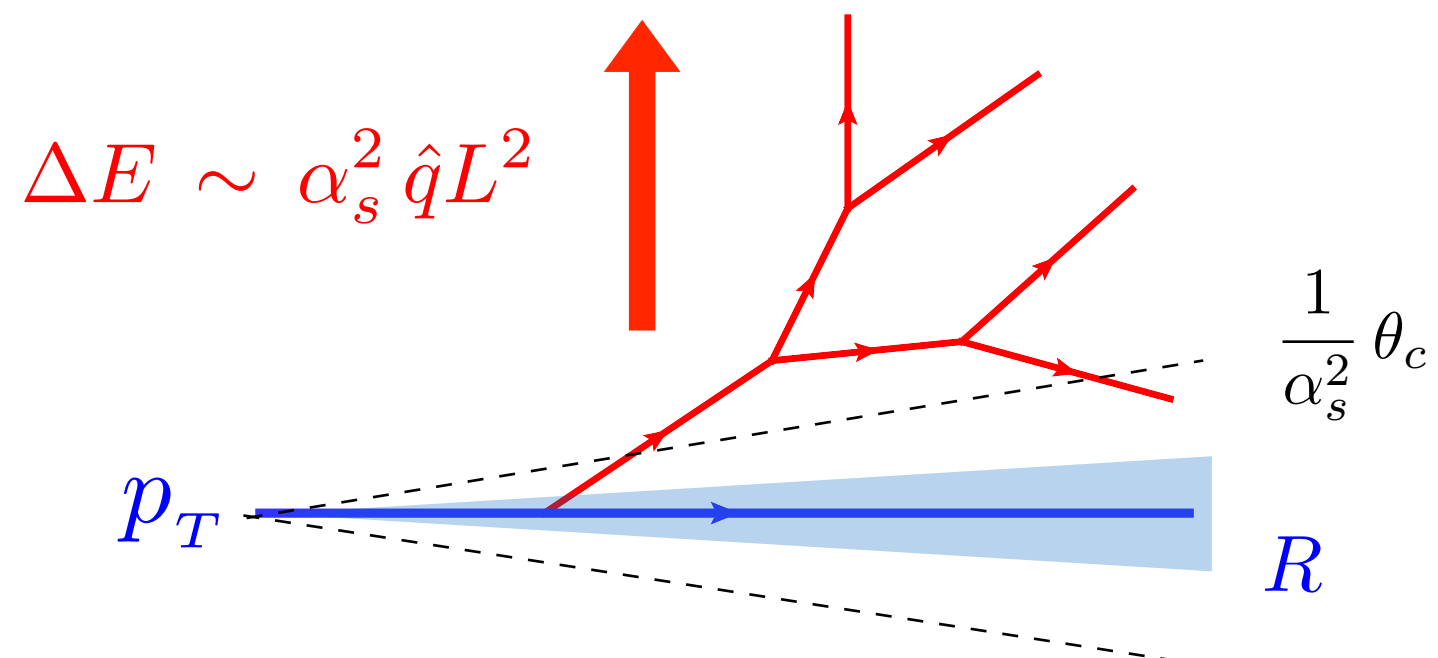
[Blaizot, Iancu, Fister, Torres, MT (2013-2014) Kurkela, Wiedemann (2014)]

- Multiple branchings at parametrically large angle

$$\theta_{\text{br}} \gg \frac{1}{\alpha_s^2} \theta_c \gg R$$

- Constant energy flow from jet energy scale  $p_T$  energy down to the medium temperature scale  $\omega \sim T$

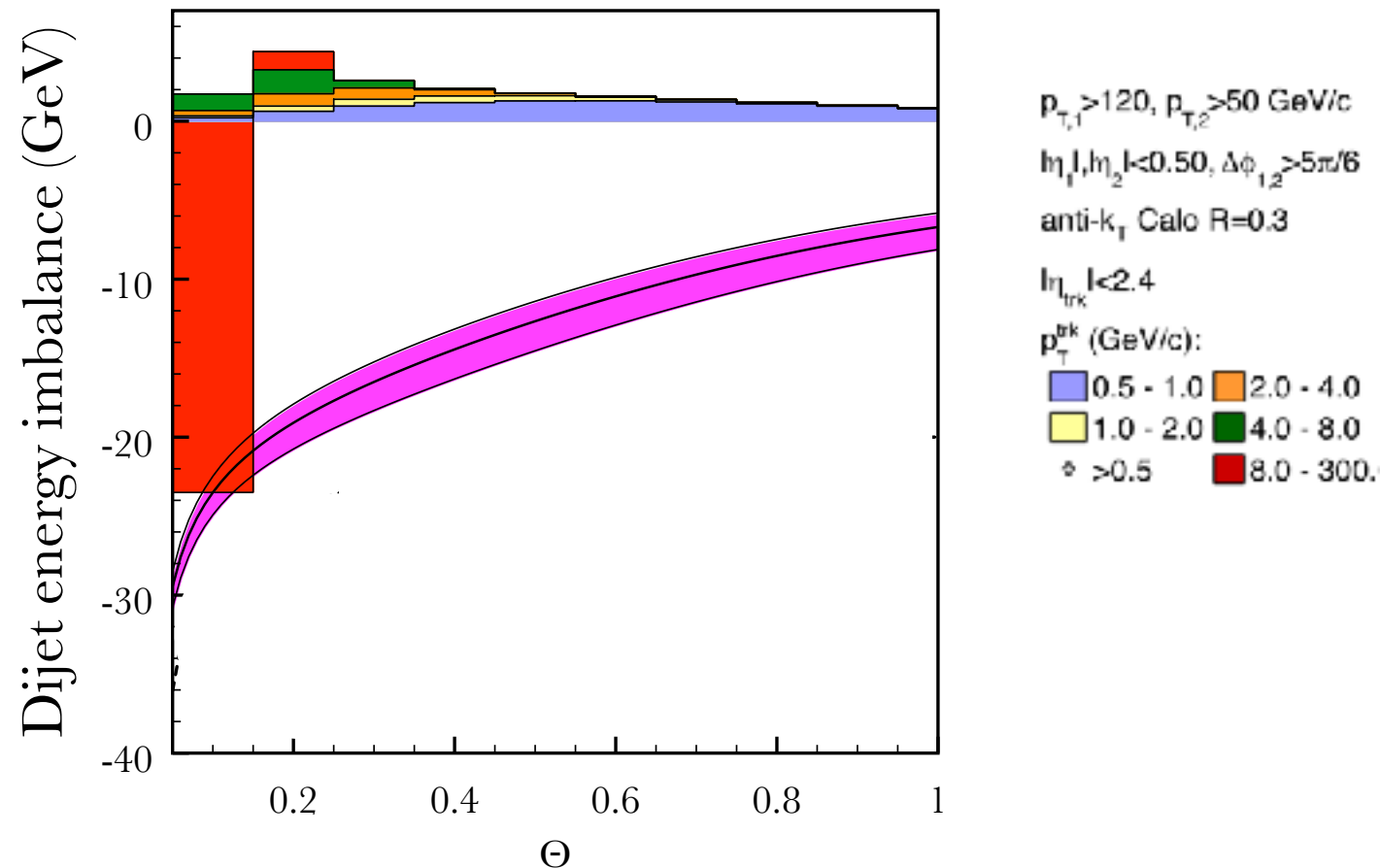
Energy lost to the medium:



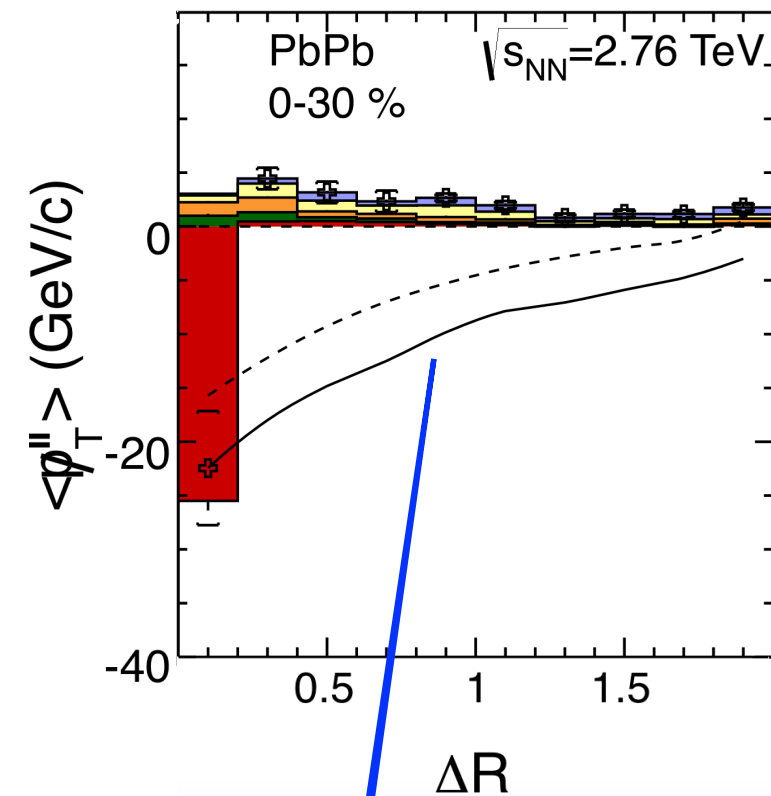
# Recovering the missing jet energy

Turbulent transport of energy to large angles

[Blaizot, MT, Torres PRL (2014)]



Might explain missing  $p_T$  in dijet events  
(CMS 2011-2014)



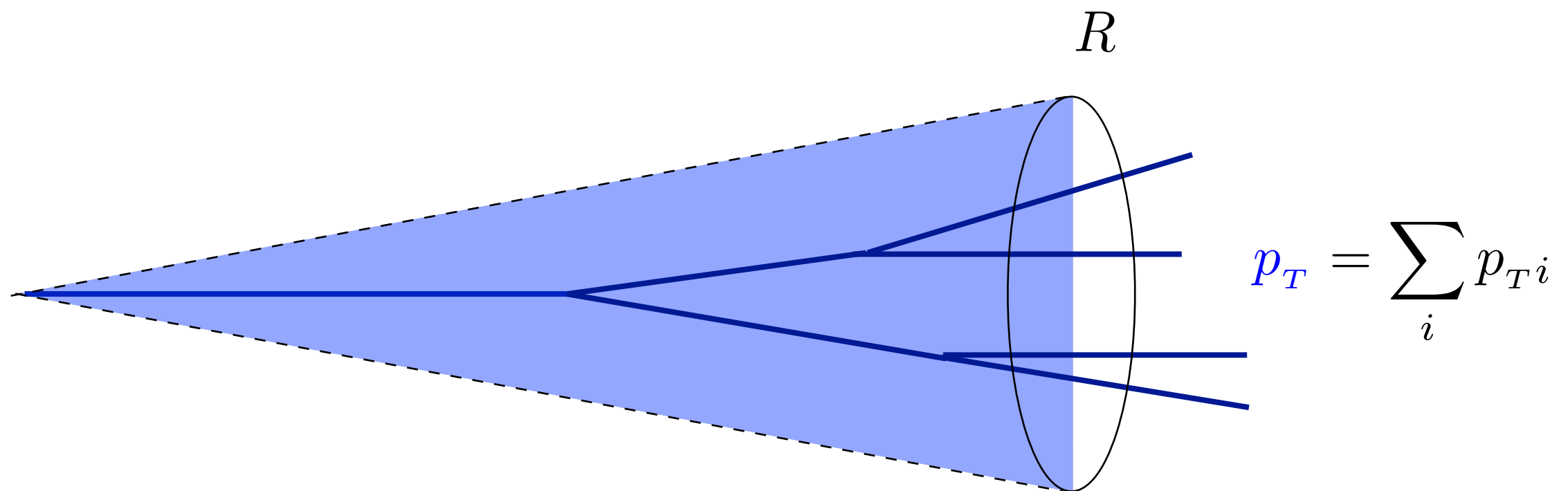
The energy lost is recovered at very large angle

How does energy loss  
depend on jet substructure?

# Jet quenching and fluctuations

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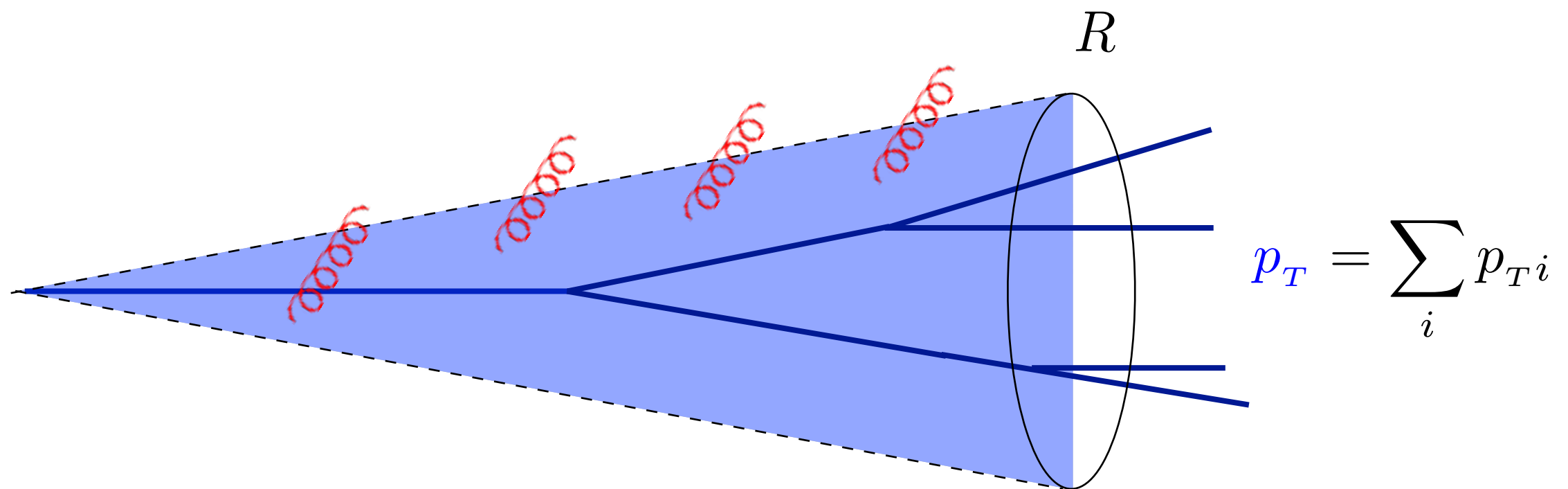
- Jets are multi-parton systems
- Not uniquely defined. Depend on inputs such as the cone size  $R$ , reconstruction algorithms (C/A, kt, anti-kt, etc) ...



# Jet quenching and fluctuations

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- Jet energy loss depend on the number of resolved color charges
- Need to account for fluctuations of energy loss due to fluctuation in the jet substructure



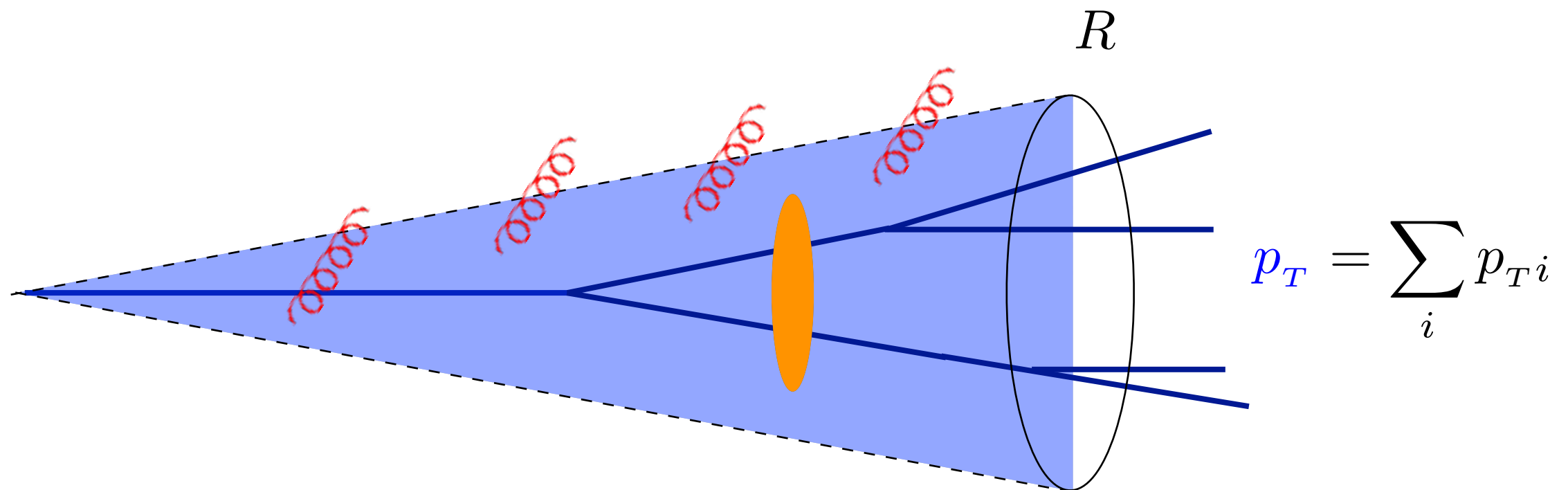


# Jet quenching and fluctuations

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Two limiting scenarios for jet energy loss

- (i) coherent Eloss, as a single color charge (parton)
- (ii) incoherently as multiple charges

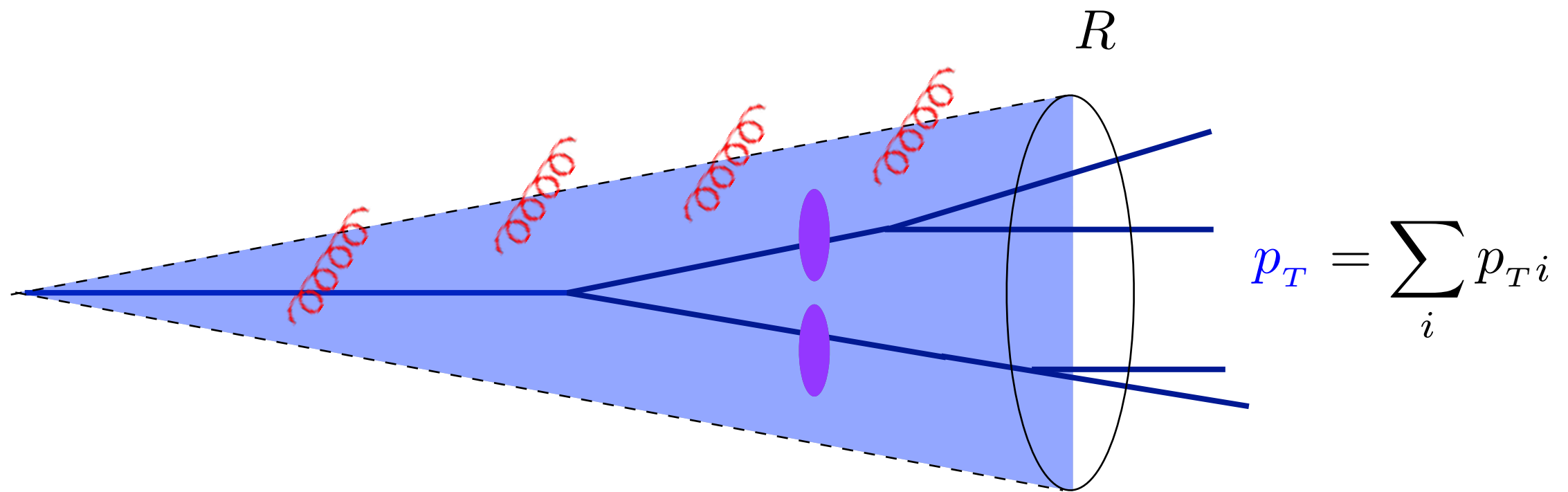


# Jet quenching and fluctuations

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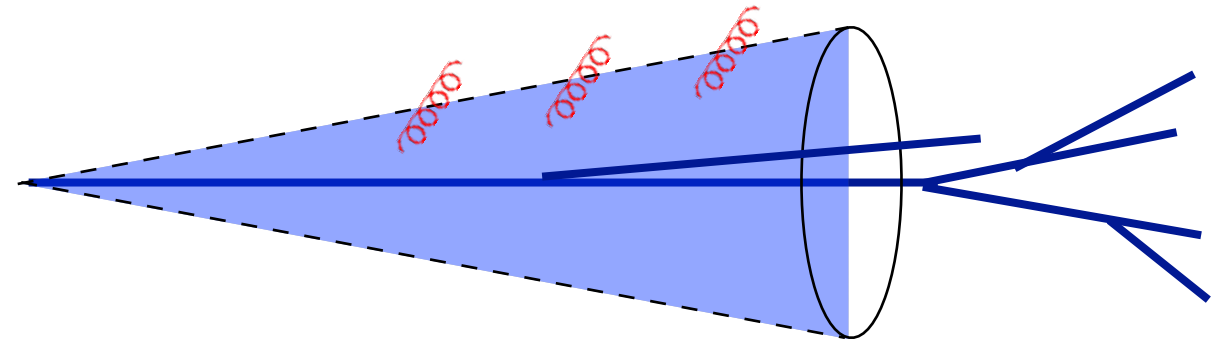


# Coherent limit of QCD

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- A large fraction of parton splittings are collinear or soft and hence occur outside the medium

$$t_{\text{form}} = \frac{1}{\omega\theta^2} > L$$

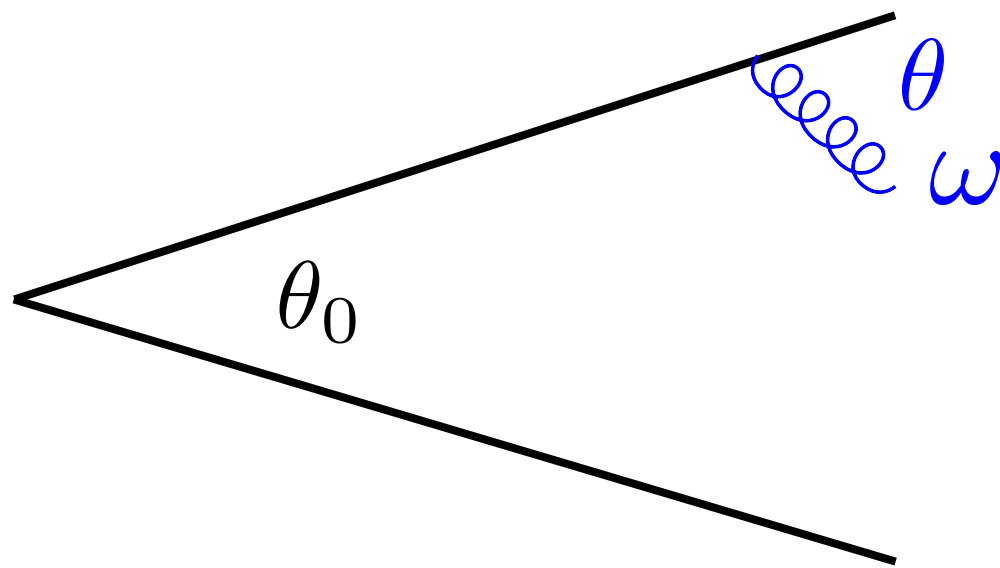


- Some parton split inside the medium at small enough angle so that the medium on average does not resolve the two individual charges
- Hence, single parton energy loss approximation applies when the jet cone size  $R$  is small enough (but compared to what? what are the relevant scales?)

# Color decoherence: the antenna setup

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- The radiation spectrum of a color singlet antenna reads



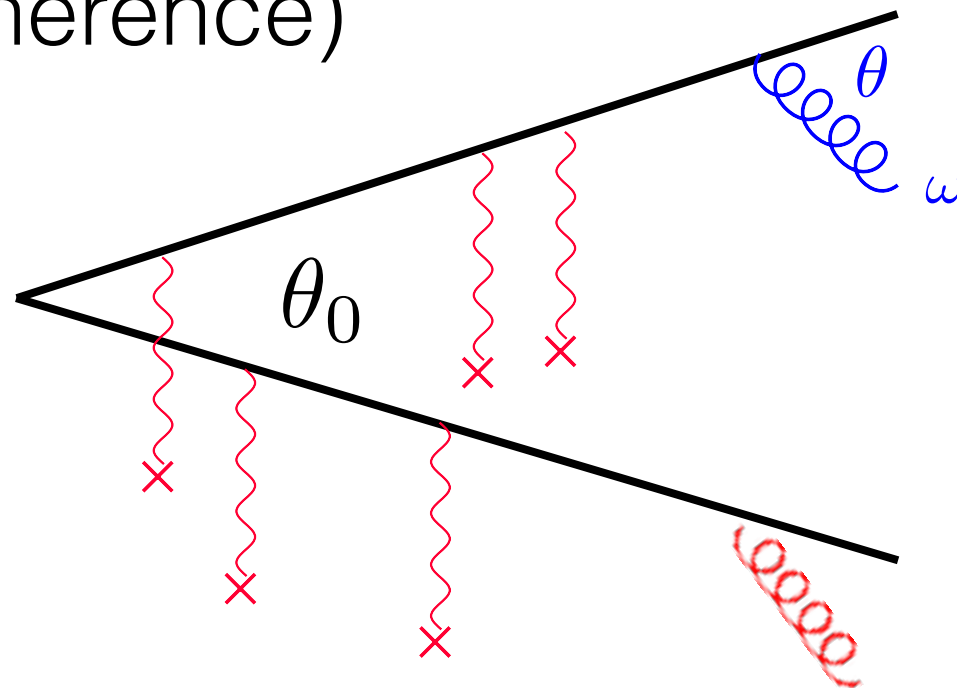
Suppression of large angle radiation due to color coherence

$$\omega \frac{dI}{d\omega d\theta} = \frac{\alpha_s C_R}{\pi \theta} \Theta(\theta_0 - \theta)$$

- Building block for QCD jet evolution (corrects virtuality evolution with angular ordering)

# Color decoherence: the antenna setup

- The presence of a colored medium causes rapid color randomization of the pair altering the radiation pattern (decoherence)



MT, Salgado, Tywoniuk PRL (2011), PLB (2012), JHEP (2011-2012)  
 Casalderrey-Solana, Iancu JHEP (2012)  
 Casalderrey-Solana, MT, Salgado, Tywoniuk PLB (2013)

more radiation off individual charges at large angle when

$$\theta_0 > \theta_c$$

$$\omega \frac{dI}{d\omega d\theta} = \frac{\alpha_s C_R}{\pi \theta} [\Theta(\theta_0 - \theta) + \Delta_{\text{med}} \Theta(\theta - \theta_0)]$$

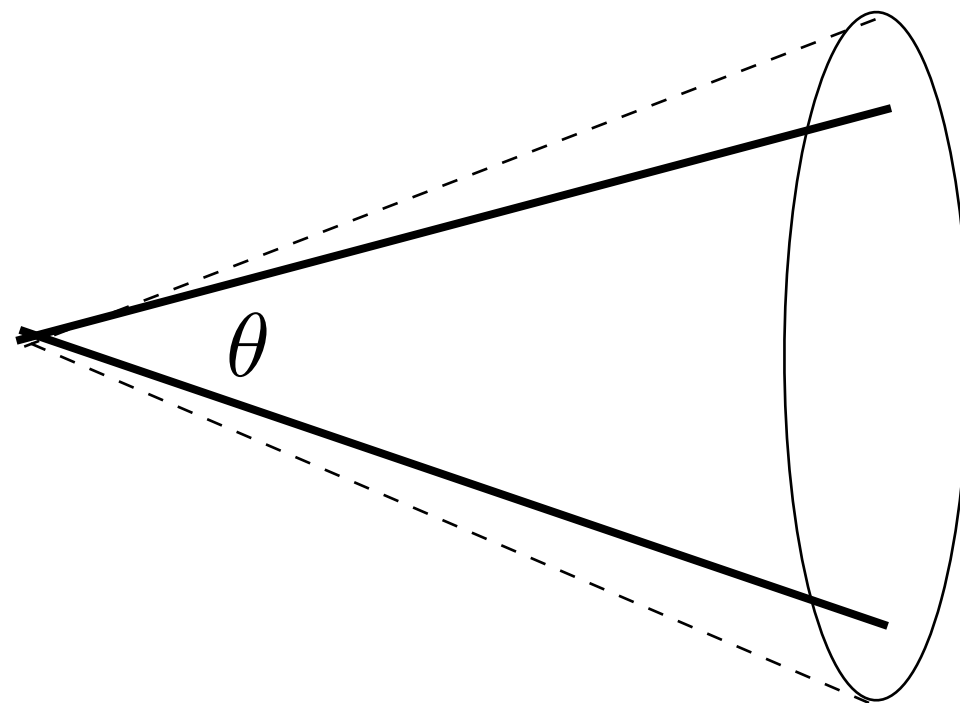
$$\Delta_{\text{med}} = 1 - e^{-\frac{1}{12} (\theta_0 / \theta_c)^2} \quad \begin{cases} 1 & \theta_0 \gg \theta_c \equiv 1 / \sqrt{\hat{q} L^3} \\ 0 & \theta_0 \ll \theta_c \end{cases}$$

decoherence parameter

# Probing color decoherence

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Investigate energy loss of a subset of jets characterized by an early hard and relatively wide angle splitting (short formation time)

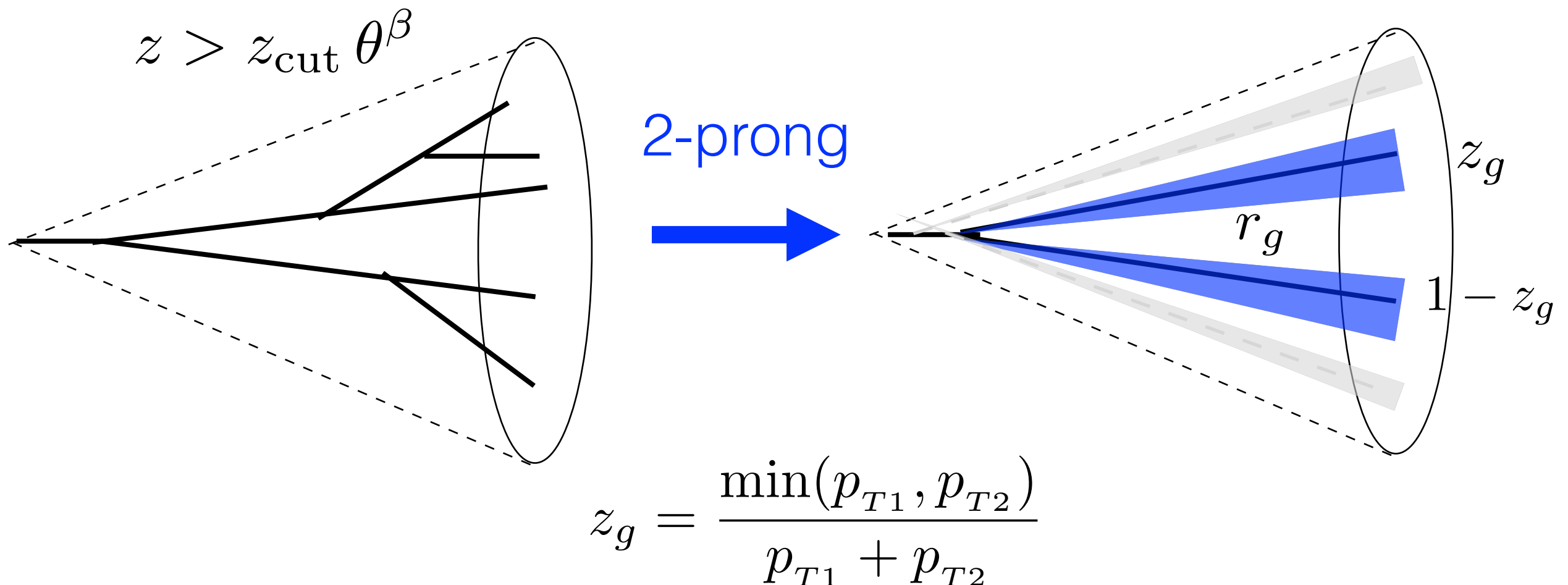


# Jet grooming techniques (SoftDrop)

- Use SoftDrop de-clustering grooming technique developed to reduce the soft contamination from PileUp and UE in order to identify events with boosted W, Z, Higgs, etc)

Identify the first splitting that passes the cut

Dasgupta, Fregoso, Marzani, Salam JHEP (2013)  
Larkoski, Marzani, Soyez, Thaler JHEP (2014)  
Larkoski, Marzani, Thaler PRD (2015)

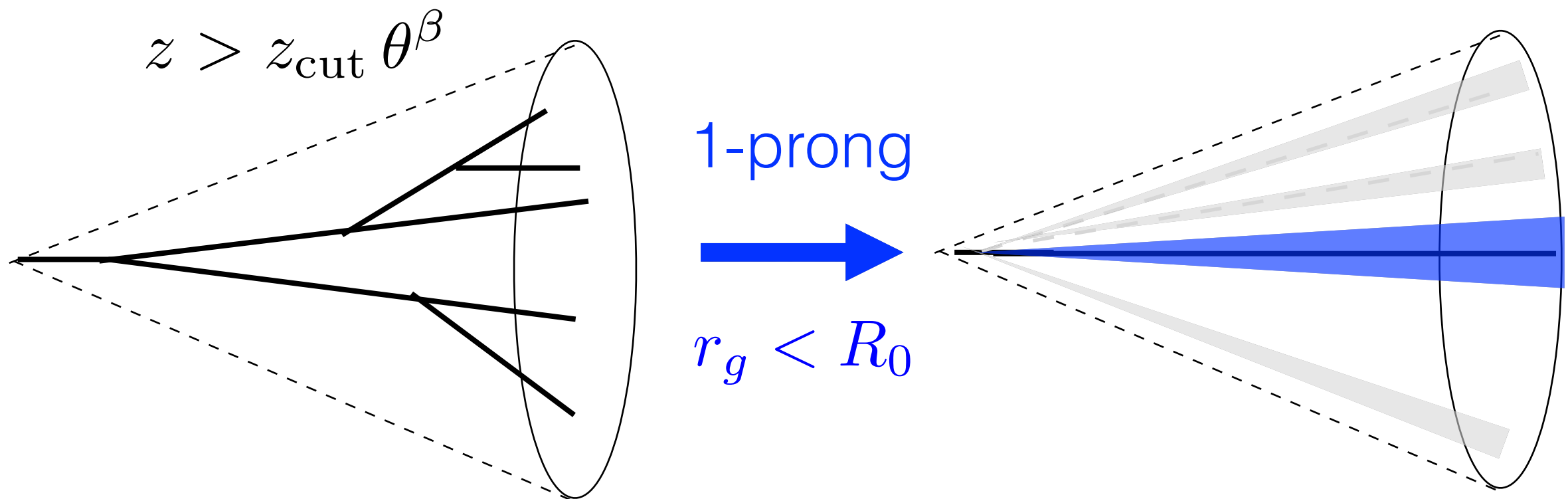


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Experimental angular resolution scale ( $R_0=0.1$  CMS):  
a fraction of jets is made of one-pronged



# Jet grooming techniques (SoftDrop)

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- In the Modified Leading Log Approximation

$$p(z_g) = \underbrace{\bar{\alpha} \int_0^R \frac{d\theta}{\theta} \Delta(R, \theta) P(z_g)}_{\text{2-prong probability}} + \underbrace{\Delta(R, R_0) \delta(1 - z_g)}_{\text{1-prong probability}}$$

- Sudakov form factor:

$\Delta(R, \theta)$  : Probability not to radiate in  $[R, \theta]$

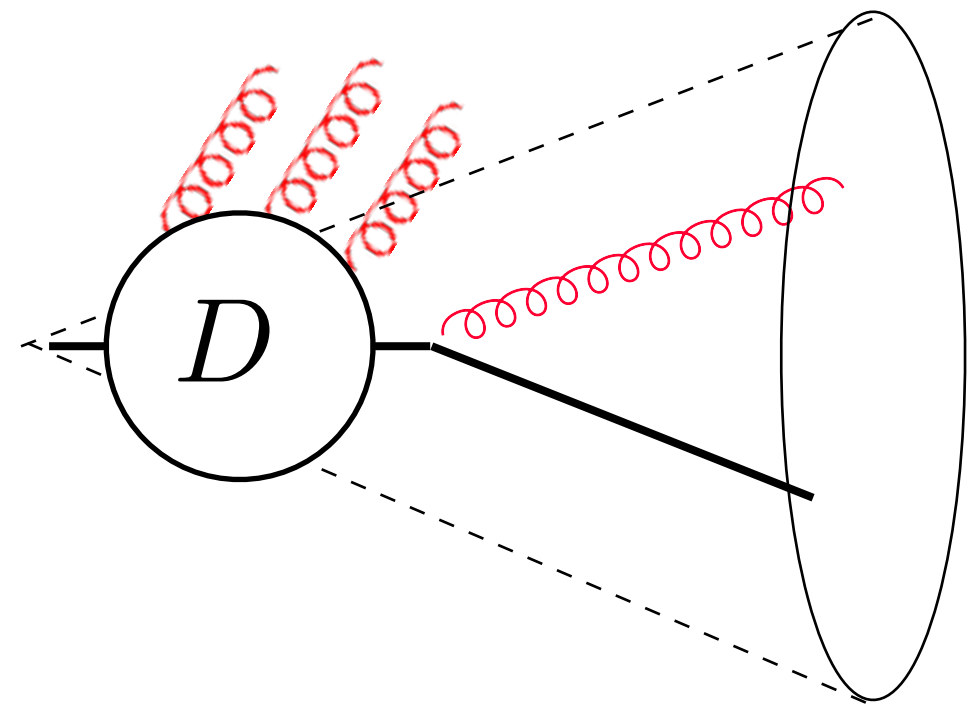
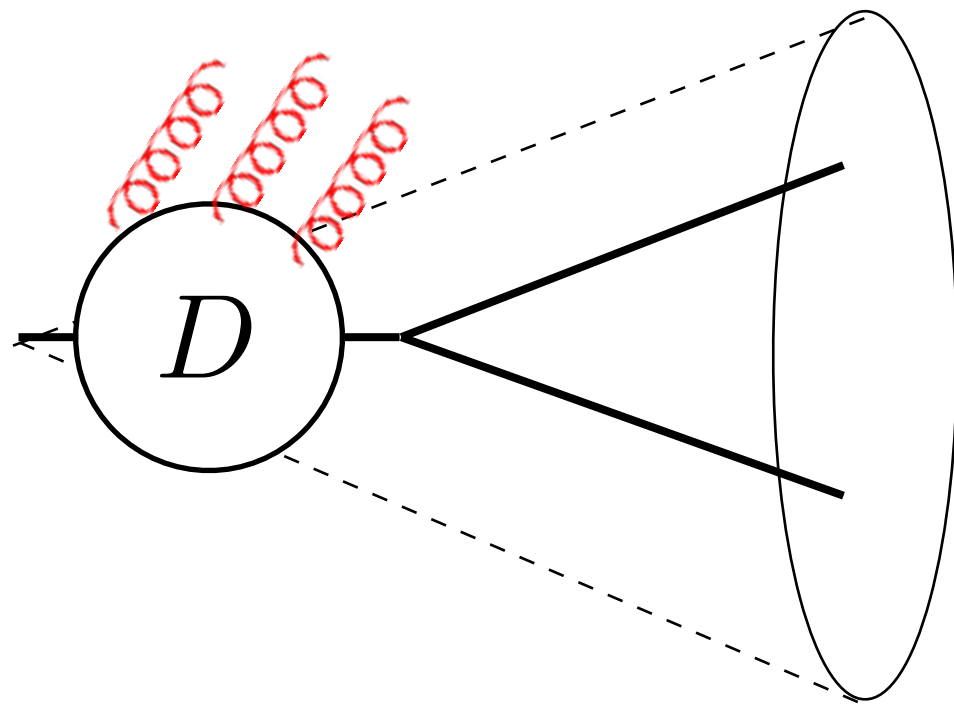
- The z-distribution measures the QCD splitting function

$$p(z_g) \sim P(z_g) \sim 1/z_g$$

# How does a 2-pronged structure lose energy?

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- In the **coherent limit**: modification may then come from in-cone:
  1. medium-induced **hard gluon radiation**
  2. reclustered soft radiation or recoil medium partons (**not easily handled analytically**)

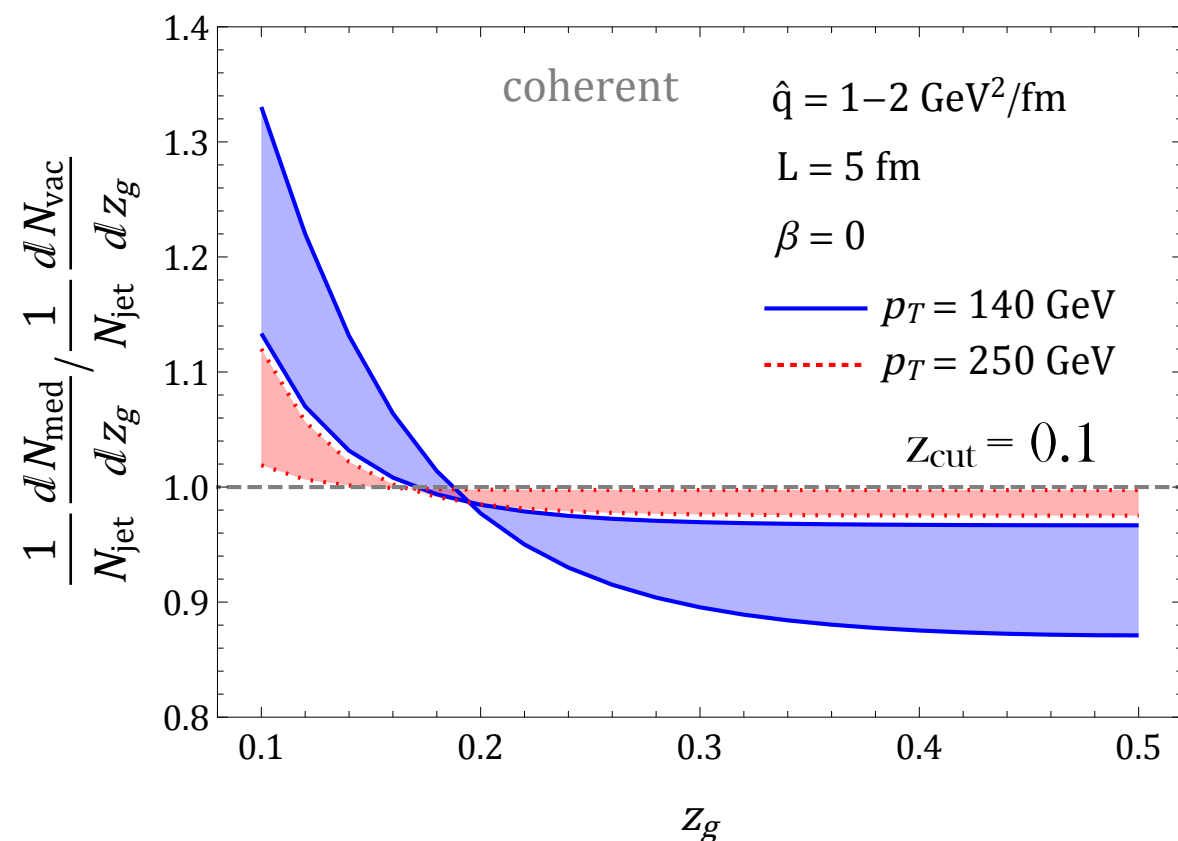


⇒ Expect enhancement of the 2-pronged probability

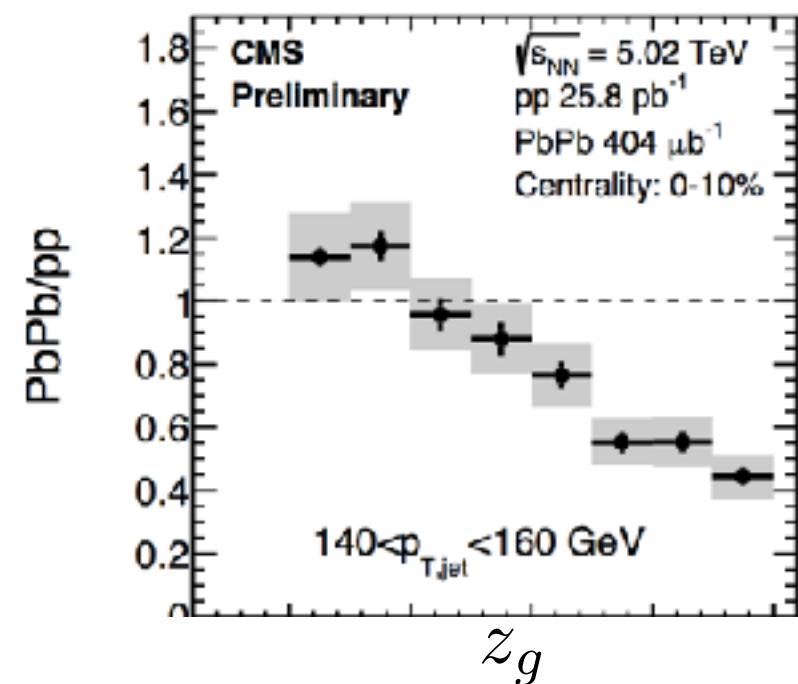
# How does a 2-pronged structure lose energy?

- **Coherent limit:** enhancement of the  $z_g$ -spectrum at small energies
- Possibility to measure **hard medium radiation**

MT, Tywoniuk, arXiv:1610.08930



Self-normalized  $p(z_g)$  ratio



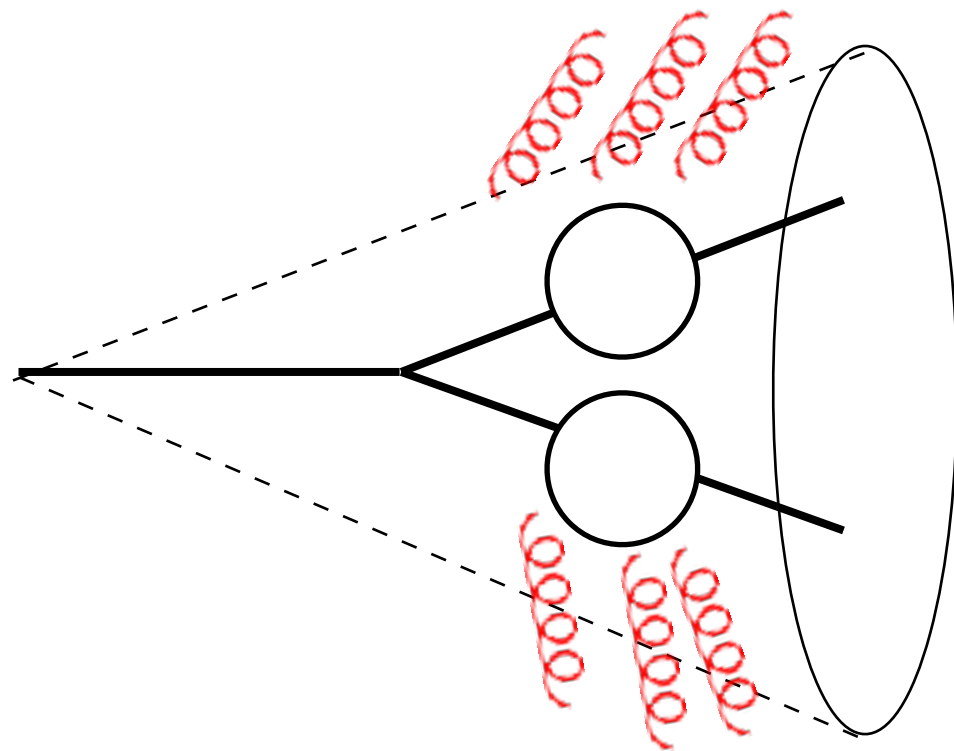
Agrees with data...but what about decoherence?

More information in the yields (2-prong  $R_{AA}$ )

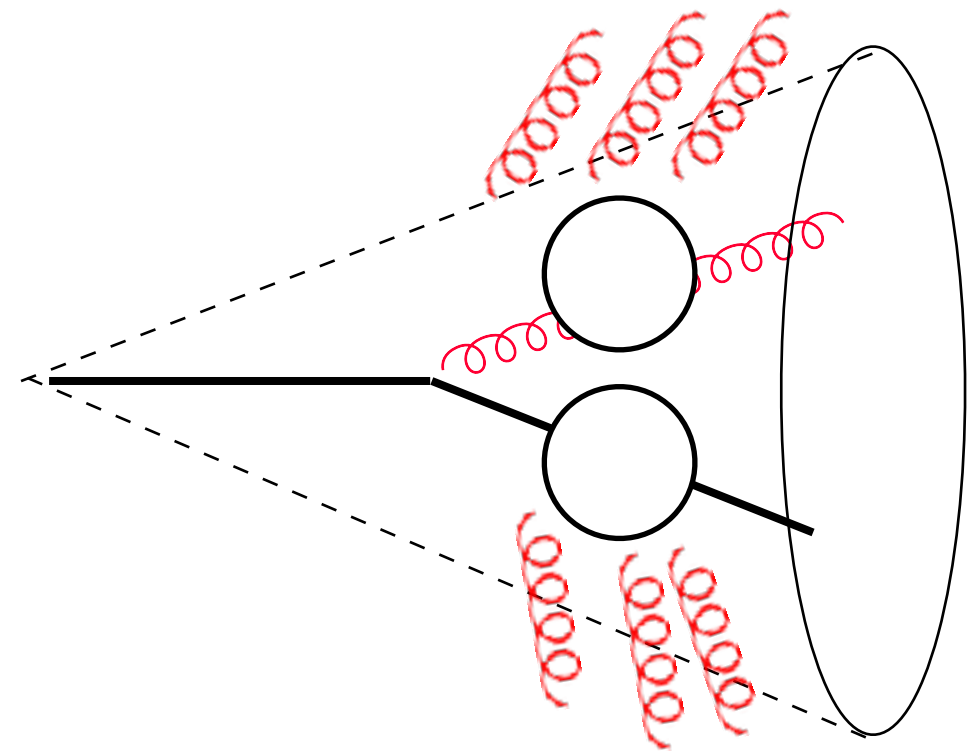
# How does a 2-pronged structure lose energy?

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- **Incoherent limit:** the two subjects lose energy independently
- In this case two pronged structures are expected to be suppressed as compared to proton-proton collisions



vacuum splitting



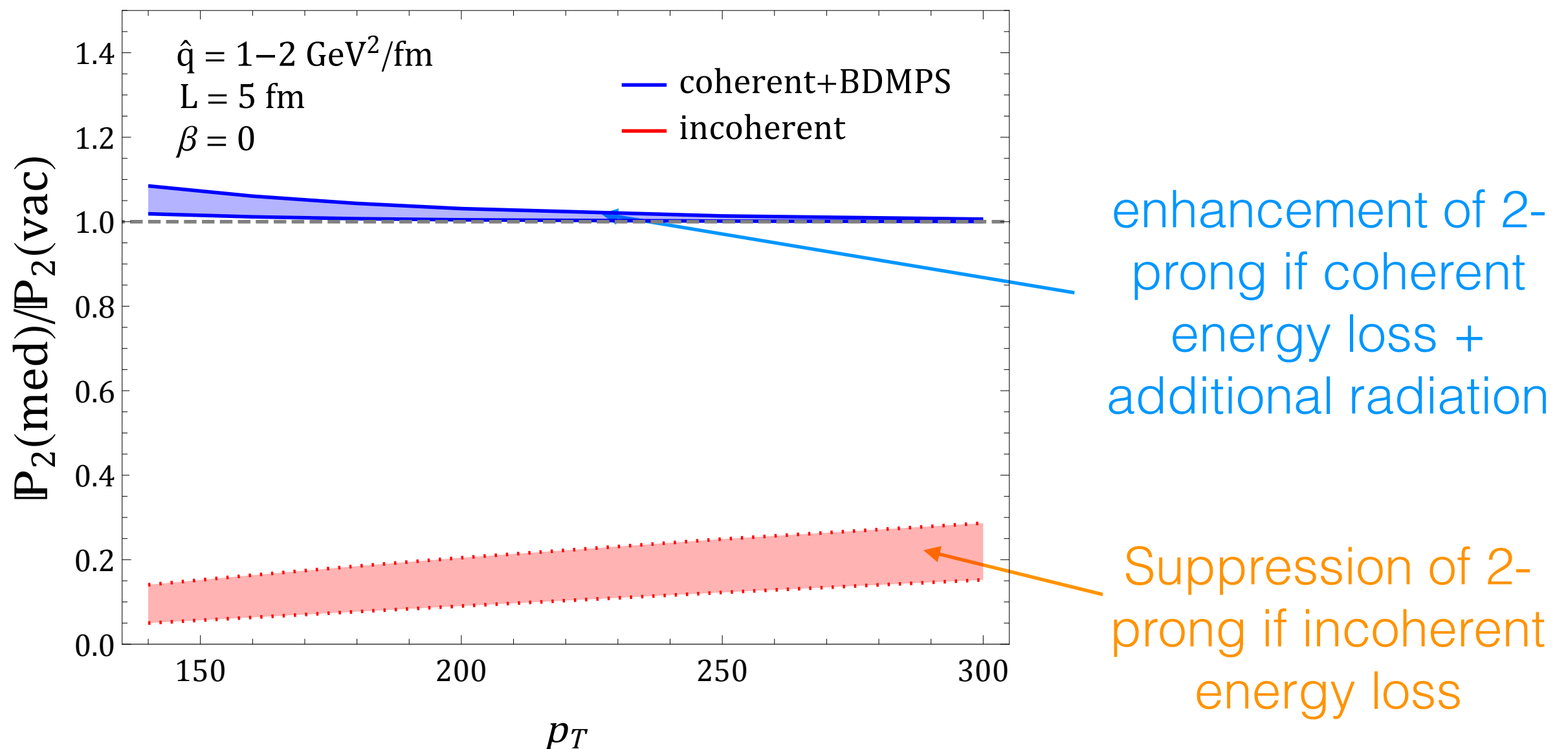
Hard medium-  
induced splitting

# How does a 2-pronged structure lose energy?

- Two-pronged probability

MT, Tywoniuk, arXiv:1610.08930

$$\mathbb{P}_{2\text{-prong}} \equiv \int_{R_0}^R dr_g \int_{z_{\text{cut}}} dz_g p(r_g, z_g)$$



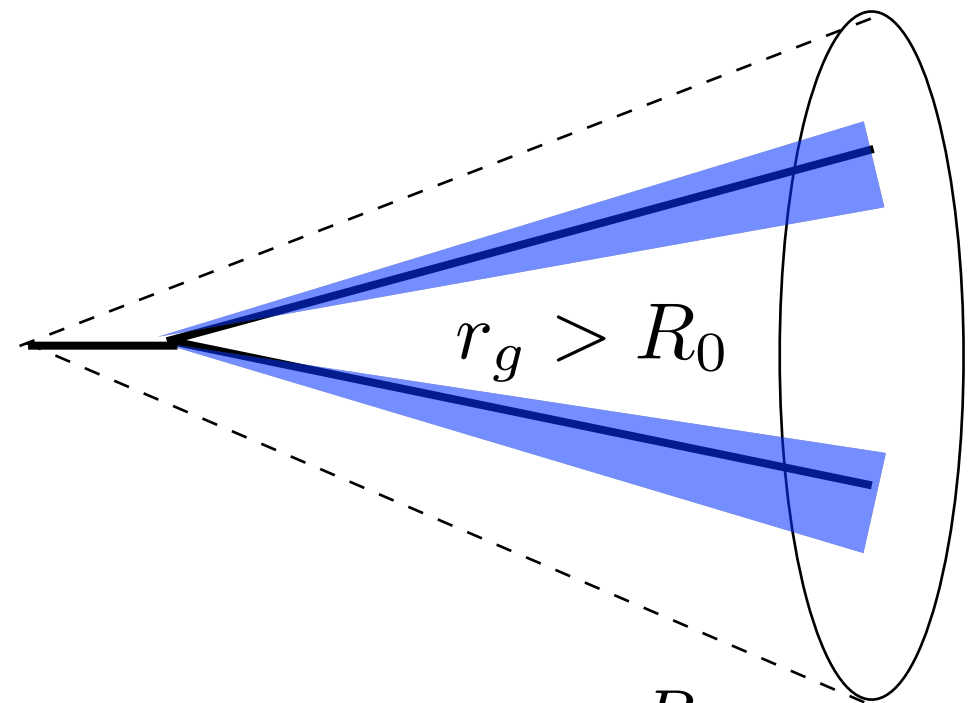
# Probing decoherence: angular distribution

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- Complementary observable to the self-normalized  $z_g$ -distribution measured by CMS [CMS-PAS-HIN-16-006]:

angular distribution of 2-pronged substructures

$$R^{2\text{-prong}} \equiv \frac{p_{AA}(r_g)}{p_{pp}(r_g)}$$



- NB: here  $p(r)$  is not self normalized!
- Probability conservation:

$$\mathbb{P}_{2\text{-prong}} + \mathbb{P}_{1\text{-prong}} = 1$$

$$\mathbb{P}_{2\text{-prong}} = \int_{R_0}^R dr_g p(r_g)$$

[See also  $N=1$  self-normalized dist.  
Vitev, Chien arXiv:1608.07283]

# Probing decoherence: angular distribution

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- Interpolation between the **coherent** and **decoherent** limits at LO:

$$\frac{dN_{2\text{-prong}}}{dp_T^2 dr_g} = (1 - \Delta_{\text{med}}(r_g)) \frac{dN_{\text{coh}}}{dp_T^2 dr_g} + \Delta_{\text{med}}(r_g) \frac{dN_{\text{decoh}}}{dp_T^2 dr_g}$$

- The 2-pronged angular probability distribution:  $p(r_g) \simeq \frac{\frac{dN_{2\text{-prong}}}{dp_T^2 dr_g}}{\frac{dN}{dp_T^2}}$
- Again, probability conservation yields

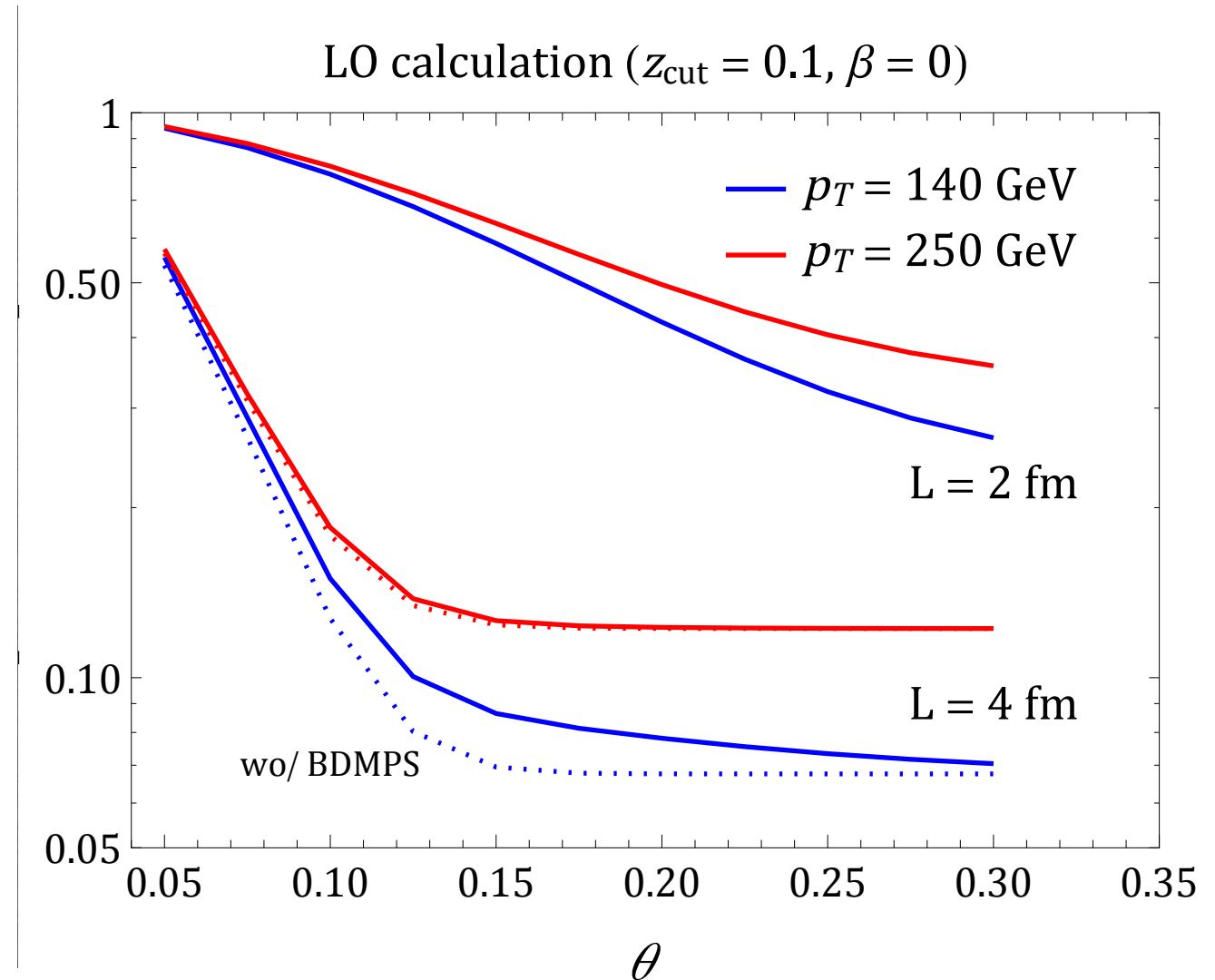
Inclusive jet spectrum

$$\frac{dN}{dp_T^2} = \int_{R_0}^R dr_g \frac{dN_{2\text{-prong}}}{dp_T^2 dr_g} + \frac{dN_{1\text{-prong}}}{dp_T^2}$$

# Probing decoherence: angular distribution

- Interpolation between the **coherent** and **decoherent** limits

$$R^{2\text{-prong}} \equiv \frac{p_{AA}(r_g)}{p_{pp}(r_g)}$$



Strong suppression of 2-pronged probability at large angle (decoherence effects  $\Rightarrow$  jet collimation)



# Summary

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- Jet substructure studies provide new tools to investigate energy loss mechanisms and color decoherence
- The angular distribution probability of two-pronged structures may provide additional information regarding the transition from the coherence to the decoherence regimes
- *caveat*: sensitivity to background contamination. Investigate jet observables that are less sensitive to possible contamination from soft radiation and recoil partons